

$$32) \quad 4x^4 - 8x^3 - 19x^2 + 23x - 6$$

deg 4 same

EB

$$\lim_{x \rightarrow \infty} f(x) = \infty$$

$$\lim_{x \rightarrow -\infty} f(x) = \infty$$

graph (d)

check
 $f(-2) = 0$

$$68) \quad V = 2666x - 210x^2 + 4x^3$$

$$V = 4x^3 - 210x^2 + 2666x$$

$$2x(2x^2 - 105x + 1333)$$

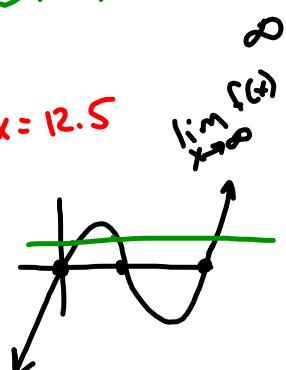
$$\frac{2666}{2} \quad \frac{2666}{1333}$$

$$QF \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad x = 31 \text{ or } 21.5$$

$$67) \quad V_1 = x(10 - 2x)(25 - 2x) \quad x=0 \quad x=5 \quad x=12.5$$

reasonable domain to consider

$$V_2 = 175$$



2.4 Real Zeros of Polynomial Functions

Let $f(x)$ and $d(x)$ be polynomials with the degree of f greater than or equal to the degree of d and $d(x) \neq 0$

There are unique polynomials $q(x)$ and $r(x)$ such that:

$$6 \overline{)12503}$$

$$f(x) = d(x) \cdot q(x) + r(x)$$

divisor quotient remainder

Ex 1 Polynomial Long Division

Use long division to find the quotient and remainder

when $2x^4 - x^3 - 2$ is divided by $2x^2 + x + 1$

$$\begin{array}{r}
 & x^2 - x \\
 2x^2 + x + 1 & \overline{)2x^4 - x^3 + 0x^2 + 0x - 2} \\
 - 2x^4 + x^3 + x^2 & \downarrow \\
 \hline
 - 2x^3 - x^2 + 0x & \downarrow \\
 - - 2x^3 - x^2 - 1x & \downarrow \\
 \hline
 & x - 2
 \end{array}$$

$x^2 - x + \frac{x - 2}{2x^2 + x + 1}$
 quotient remainder

THEOREM Remainder Theorem

If a polynomial $f(x)$ is divided by $x - k$, then the remainder is $r = f(k)$.

Ex 2 Using the Remainder Theorem

Find the remainder when $f(x) = 3x^2 + 7x - 20$ is divided by

| | | |
|----------------------|------------------------|------------------------|
| a) $x - 2 = 0$ | b) $x + 1$ | c) $x + 4$ |
| $f(2) = \cancel{r}$ | $f(-1)$ | $f(-4)$ |
| $3(2)^2 + 7(2) - 20$ | $3(-1)^2 + 7(-1) - 20$ | $3(-4)^2 + 7(-4) - 20$ |
| $f(2) = 6$ | $f(-1) = -24$ | $f(-4) = 0$ |

What does each mean?

THEOREM Factor Theorem

A polynomial function $f(x)$ has a factor $x - k$ if and only if $f(k) = 0$.

Ex 3 Synthetic Division

Divide $2x^3 - 3x^2 - 5x - 12$ by $x - 3$

↑ divides evenly

$$\begin{array}{r}
 3 \downarrow & 2 & -3 & -5 & -12 \\
 & \downarrow & 6 & 9 & 12 \\
 \hline
 & 2 & 3 & 4 & 0 \\
 \boxed{2x^2 + 3x + 4} & & &
 \end{array}$$

$\frac{2x^3 - 3x^2 - 5x - 12}{x - 3}$
 $x \neq 3$

p 223 # 2, 4, 5, 7, 9, 10, 14, 16, 17
 19, 21, 23, 24