Combining Transformations – Does Order Matter?

Complete the following transformations in the order given.

Ex 1: Parent function: $y = \sqrt{x}$

- a) Shift upward 3 units, then left 4 units.
- b) Shift left 4 units, then left upward 3 units.
- c) Do you get the same function from a and b?

Ex 2: Parent function: $y = \sqrt{x}$

- a) Stretch vertically by a factor of 3, then shift upward 2 units.
- b) Shift upward 2 units, then stretch vertically by a factor of 3.
- c) Do you get the same function from a and b?

Ex 3: Parent function: $y = \sqrt{x}$

- a) Reflect across the y-axis, then shift downward 3 units.
- b) Shift downward 3 units, then reflect across the y-axis.
- c) Do you get the same function from a and b?

Ex 4: Parent function: $y = \sqrt{x}$

- a) Reflect across the y-axis, then shift right 3 units.
- b) Shift right 3 units, then reflect across the y-axis.
- c) Do you get the same function from a and b?

Ex 5: Parent function: $y = \sqrt{x}$

- a) Reflect across the x-axis, then shift downward 3 units.
- b) Shift downward 3 units, then reflect across the x-axis.
- c) Do you get the same function from a and b?

Ex 6: Parent function: $y = \sqrt{x}$

- a) Shrink horizontally by a factor of $\frac{1}{5}$, then shift right 3 units.
- b) Shift right 3 units, then shrink horizontally by a factor of $\frac{1}{5}$.
- c) Do you get the same function from a and b?

Note that:

Vertical translation (up or down) → Vertical effect (V)

Horizontal translation (left or right) → Horizontal effect (H)

x-axis reflection Vertical effect (V)

Vertical stretch or shrink

→ Vertical effect (V)

Horizontal stretch or shrink → Horizontal effect (H)

Now let's look for a pattern:

Example	Transformations and Effect (V or H) in (a)	Transformations and Effect (V or H) in (b)	(a) and (b) same?
1			,, , , , , , , , , , ,
2			
3		·	
4			
5			
6			

The order of transformations did not matter in examples
The effects in those examples were:
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The effects in those examples were:

Conclusion:

When we perform two or more transformations with the same effect (V or H) the order may affect the final function. But a transformation with a vertical effect (V) and one with a horizontal effect (H) do not affect each other.

So, in which order do we perform the transformations on a given function?

(1)
$$y = 5\sqrt{x+3} - 1$$

First, identify each transformation and its effect without regard to correct order.

Which transformation(s) can be done at any point?

Which transformation(s) must be done in a specific order?

(2)
$$y = \sqrt{-x+3} - 1$$

First, identify each transformation and its effect without regard to correct order.

Which transformation(s) can be done at any point?

Which transformation(s) must be done in a specific order?